Name (Last, First)

1. (5pts) Let a  $2 \times 2$  matrix A is given by

$$\begin{bmatrix} 7 & -2 \\ 4 & 3 \end{bmatrix}.$$

Find a real matrix C of the form

$$\begin{bmatrix} a & -b \\ b & a \end{bmatrix}$$

which is similar to A.<sup>1</sup>

 $<sup>^{1}</sup>$ Of course, you should find the P as well. Please check your answer.

2. (3pts) What is the length of  $-\mathbf{x}$  (negative of  $\mathbf{x}$ )?

$$\mathbf{x} = \begin{bmatrix} 3 \\ -5 \\ -1 \\ 1 \end{bmatrix}$$

3. (2pts) Find a  $4\times 4$  matrix A which has only one eigenvalue and the eigenspace is 2-dimensional. **Explain why.**