

Name (Last, First)  

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1. Mark each statement True or False.

- a. Let  $A$  be an  $m \times n$  matrix.  
The dimension of  $\text{Col } A$  is the same as the dimension of the column space of  $A^T$ . T F
- b. Let  $\mathbb{P}_4$  be the set of polynomials of degree at most 4.  
Let  $V$  be  $\{p(x) \in \mathbb{P}_4 \text{ satisfying } p(1) = 0 \text{ and } p(0) = 1\}$ . Then,  $V$  is a vector space. T F
- c. Let  $A$  be a  $2 \times 3$  matrix and  $B$  be a  $3 \times 2$  matrix.  
If  $AB = I_2$ , then the columns of  $A$  are linearly independent. T F
- d. Let  $T$  be a linear transformation.  
The range of  $T$  is a vector space. T F
- e. Let  $V$  be a vector space of dimension  $n$ .  
A spanning set should have at least  $n$  vectors in it. T F
- f. Let  $\mathbb{R}^3$  be the vector space  $\mathbb{R}^3$ .....  
A plane in  $\mathbb{R}^3$  is a two-dimensional subspace. T F
- g. Let  $\mathcal{B}$  be a basis for a vector space.  
In some cases, the coordinate mapping  $\mathbf{x} \mapsto [\mathbf{x}]_{\mathcal{B}}$  is not onto. T F
- h. Let  $A$  be a  $n \times n$  matrix.  
The null space of  $A$  is  $\{\mathbf{0}$  (the zero vector) $\}$  if and only if  $A$  is invertible. T F